



Axions and Large Extra Dimensions

Biljana Lakić

Rudjer Bošković Institute, Zagreb

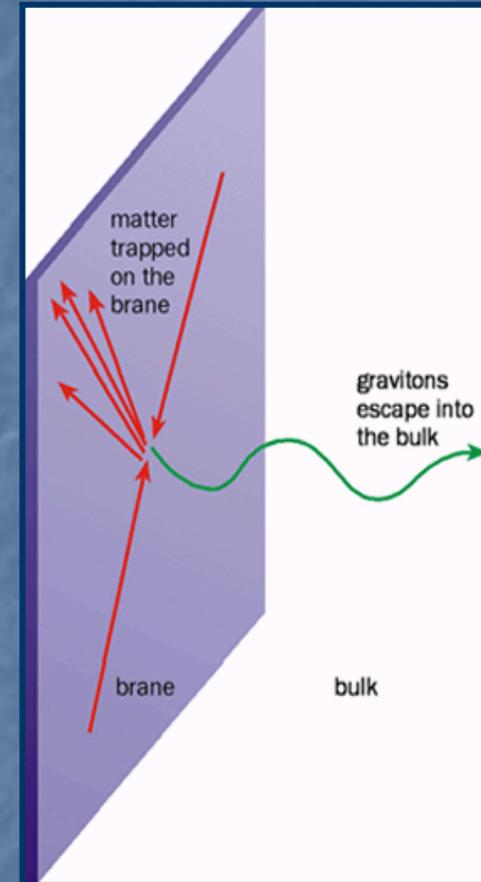
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19 - 25 June 2007, Patras

Outline

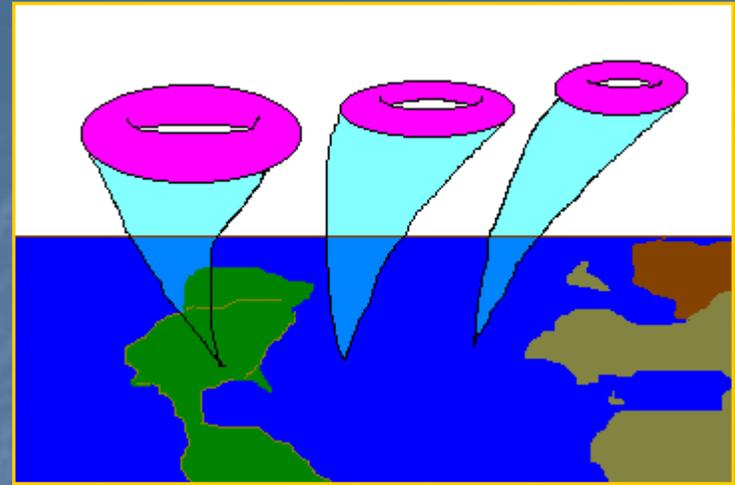
- Introduction on extra dimensions
- Axions in large extra dimensions
- CAST as a probe of large extra dimensions
- Conclusions

Extra dimensions

- possible solution to the **hierarchy problem** in particle physics (the large separation between the weak scale $M_W \sim 10^3$ GeV and the Planck scale $M_{Pl} \sim 10^{19}$ GeV)
- general ideas:
 - n extra spatial dimensions in which gravity propagates
 - Standard Model particles confined to our 3-dim. subspace
 - hierarchy generated by the geometry of additional dimensions
- testable predictions at the TeV scale



Extra dimensions



Three scenarios:

- Large extra dimensions (Arkani-Hamed, Dimopoulos, Dvali)
 - extra dimensions are compactified (a large radius of compactification) and the geometry of the space is flat
- Warped dimensions (Randall, Sundrum)
 - large curvature of the extra dimensions
- TeV^{-1} sized extra dimensions
 - Standard Model particles may propagate in the bulk

Large extra dimensions (LED)

- relation between the Planck scale and the fundamental higher-dimensional scale M_D

$$M_{\text{Pl}} \approx M_D (RM_D)^{n/2}$$

R is the compactification radius

- if $M_D \sim 1$ TeV, R ranges from \sim mm to ~ 10 fm for $n = 2-6$ ($1/R$ ranges from $\sim 10^{-4}$ eV to ~ 10 MeV)
- Standard Model fields constrained to the brane
- bulk graviton expands into a Kaluza-Klein (KK) tower of spin-2 states which have masses $\sqrt{\vec{k}^2 / R^2}$, where \vec{k} labels the KK excitation level

Large extra dimensions (LED)

Constraints on the radius of the extra dimensions, for the case of two-flat dimensions of equal radii (PDG2006):

- direct tests of Newton's law $\frac{1}{r^2} \rightarrow \frac{1}{r^{2+n}}$ for $r < R$

$$R < 0.13 \text{ mm}$$

- collider signals (direct production of KK gravitons)

$$R < 210 - 610 \text{ } \mu\text{m}$$

- astrophysics (limits depend on technique and assumption)

- supernova cooling $R < 90 - 660 \text{ nm}$

- neutron stars $R < 0.2 - 50 \text{ nm}$

Axions in LED

- axions could also propagate in $\delta \leq n$ extra dimensions. **Why?**
 - axions are singlets under the Standard Model gauge group
 - to avoid a new hierarchy problem M_W vs. f_{PQ}
- interesting predictions:
 - tower of Kaluza-Klein states
 - lowest KK excitation specifies the coupling strength of each KK state to matter
 - given source (the Sun) will emit axions of each mode up to the kinematic limit
 - **axion mass may decouple from the Peccei-Quinn scale !**
(in 4-dimensional theory $m_{PQ} \sim 1/f_{PQ}$)

Axions in LED

- relation between the higher-dimensional and 4-dimensional scale (M_s is a fundamental mass scale, e.g. a type I string scale)

$$f_{\text{PQ}}^2 \approx \bar{f}_{\text{PQ}}^2 M_S^\delta R^\delta$$

- for gravity $M_{\text{Pl}} \approx M_D (RM_D)^{n/2}$

- Kaluza-Klein decomposition of the axion field (upon compactification of one extra spatial dimension)

$$a(x^\mu, y) = \sum_{n=0}^{\infty} a_n(x^\mu) \cos\left(\frac{ny}{R}\right)$$

- effective 4-dimensional Lagrangian

$$L_{\text{eff}} = L_{\text{QCD}} + \frac{1}{2} \sum_{n=0}^{\infty} (\partial_\mu a_n)^2 - \frac{1}{2} \sum_{n=1}^{\infty} \frac{n^2}{R^2} a_n^2 + \underbrace{\frac{\xi}{f_{\text{PQ}}} \frac{g^2}{32\pi} \left(\sum_{n=0}^{\infty} r_n a_n \right)}_{\text{KK modes are not mass eigenstates}} F_a^{\mu\nu} \tilde{F}_{\mu\nu}$$

KK modes are not mass eigenstates

Axions in LED

The mass matrix:

K. R. Dienes, E. Dudas, T. Gherghetta,
Phys. Rev. D 62, 105023 (2000)

$$M^2 = m_{\text{PQ}}^2 \begin{pmatrix} 1 & \sqrt{2} & \sqrt{2} & \sqrt{2} & \dots \\ \sqrt{2} & 2+y^2 & 2 & 2 & \dots \\ \sqrt{2} & 2 & 2+4y^2 & 2 & \dots \\ \sqrt{2} & 2 & 2 & 2+9y^2 & \dots \\ \vdots & \vdots & \vdots & \vdots & \ddots \end{pmatrix} \quad y = \frac{1}{m_{\text{PQ}} R}$$

The mass eigenvalues:

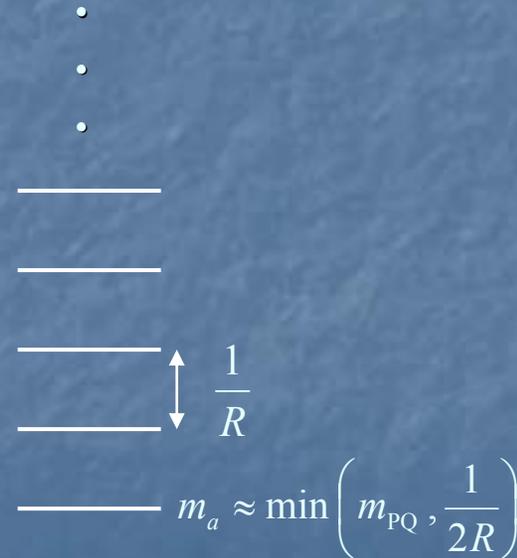
1) $m_{\text{PQ}}, \frac{1}{R}, \frac{2}{R}, \dots$ for $m_{\text{PQ}} \ll \frac{1}{R}$

2) $\frac{1}{2R}, \frac{3}{2R}, \frac{5}{2R}, \dots$ for $m_{\text{PQ}} \gg \frac{1}{R}$

- the lightest axion mass eigenvalue

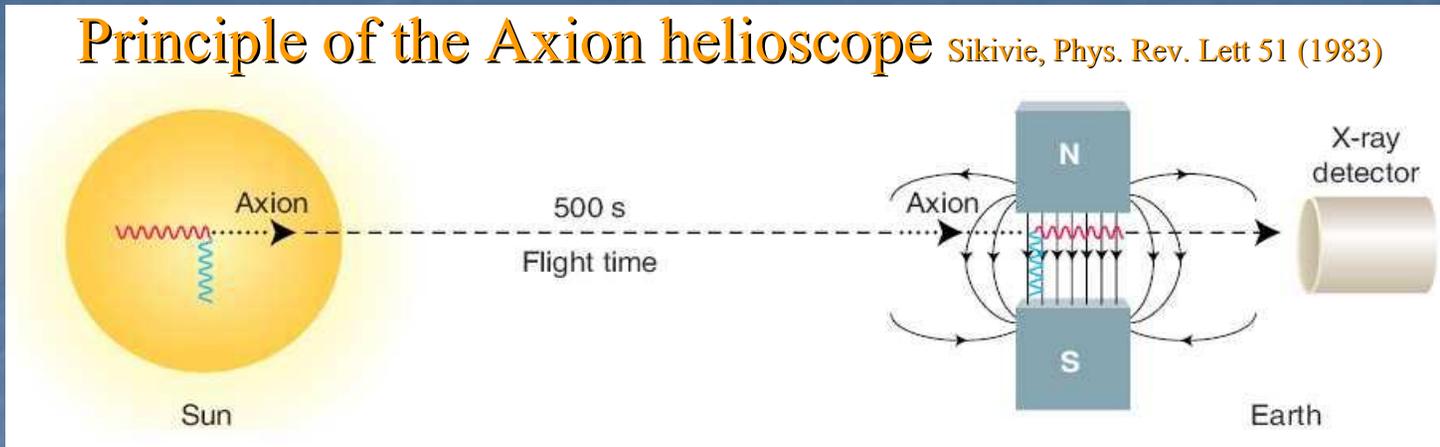
$$m_a \approx \min \left(m_{\text{PQ}}, \frac{1}{2R} \right)$$

- the masses of KK excitations are separated by $\approx 1/R$

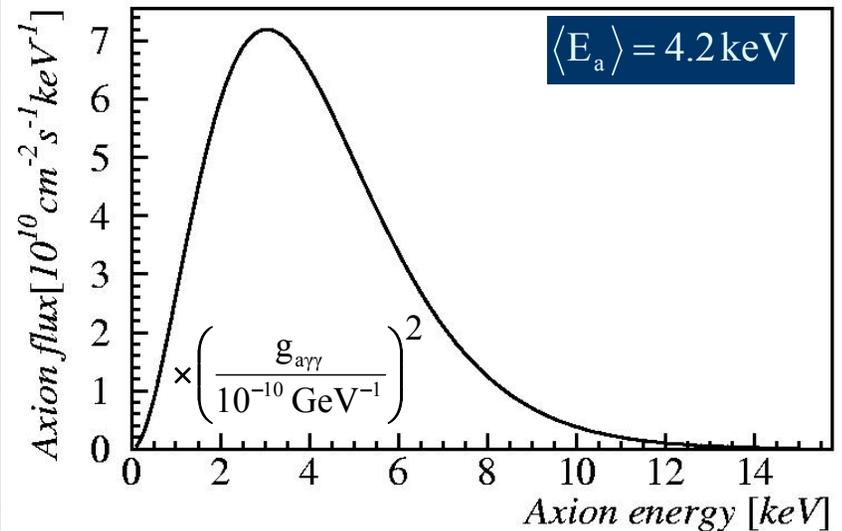


CAST: Physics

Principle of the Axion helioscope Sikivie, Phys. Rev. Lett 51 (1983)



differential axion flux at the Earth



- expected number of photons

$$N_\gamma = \int \frac{d\Phi_a}{dE_a} P_{a \rightarrow \gamma} S t dE_a$$

CAST: Physics

- conversion probability in gas (in vacuum: $\Gamma=0$, $m_\gamma=0$)

$$P_{a \rightarrow \gamma} = \left(\frac{Bg_{a\gamma\gamma}}{2} \right)^2 \frac{1}{q^2 + \Gamma^2/4} \left[1 + e^{-\Gamma L} - 2e^{-\Gamma L/2} \cos(qL) \right]$$

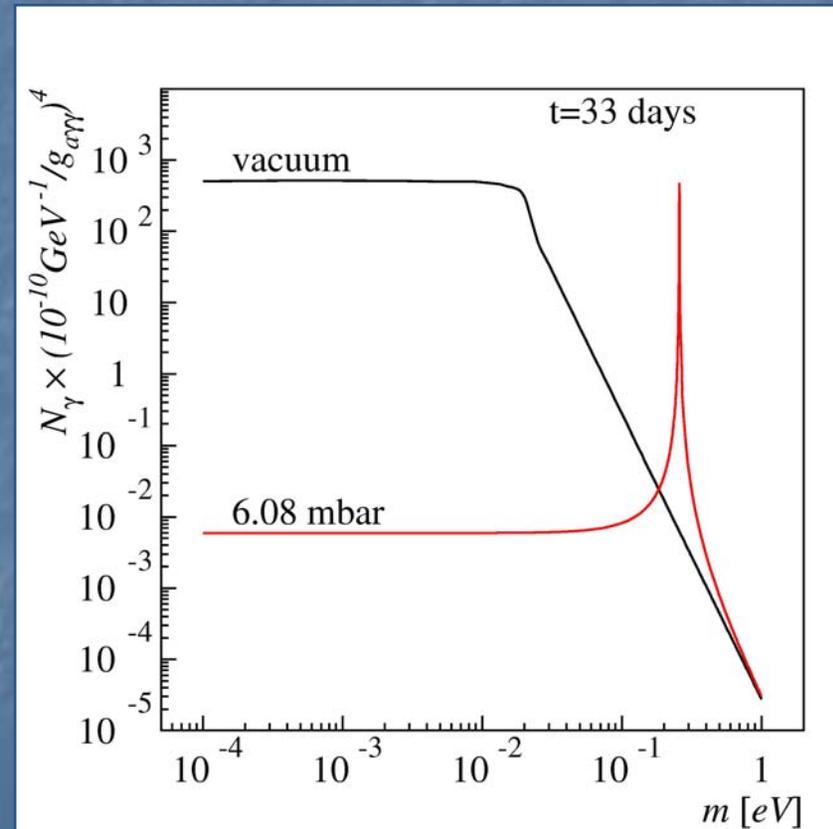
L =magnet length, Γ =absorption coeff.

$$q = \left| \frac{m_\gamma^2 - m^2}{2E_a} \right| \quad \text{axion-photon momentum transfer}$$

$$m_\gamma \text{ (eV)} \approx \sqrt{0.02 \frac{P \text{ (mbar)}}{T \text{ (K)}}} \quad \text{effective photon mass} \quad (T=1.8 \text{ K})$$

- coherence condition

$$qL < \pi \Rightarrow \sqrt{m_\gamma^2 - \frac{2\pi E_a}{L}} < m < \sqrt{m_\gamma^2 + \frac{2\pi E_a}{L}}$$



CAST as a probe of LED

$$n = 2$$

since CAST is sensitive to axion masses up to ~ 1 eV

1) **limits on the coupling constant** (we use $R \leq 0.15$ mm $\Rightarrow 1/R = 1.3 \times 10^{-3}$ eV)

- estimated number of X-rays at the pressure P_i

$$N_{\gamma i}^{KK} = \frac{2\pi^{\delta/2}}{\Gamma(\delta/2)} R^\delta \int_0^\infty dm m^{\delta-1} N_{\gamma i}(m) G(m) \quad N_{\gamma i}(m) = \int \frac{d\Phi_a(m)}{dE_a} S t_i P_{a \rightarrow \gamma i}(m)$$

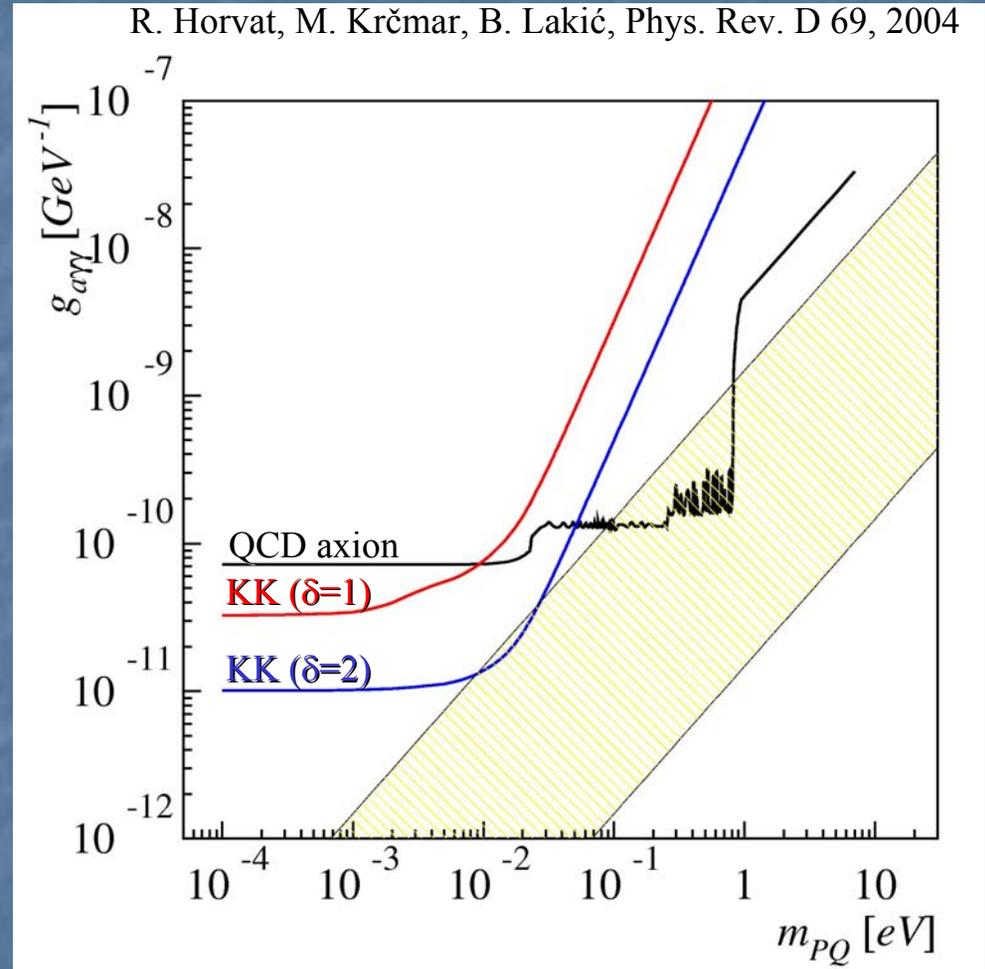
- function $G(m)$ arises from the **mixing between the KK axion modes** \Rightarrow rapid **decoherency** of the linear combination of KK axion states which couples to Standard Model fields

$$G(m) = \tilde{m}^4 \left(\tilde{m}^2 + 1 + \frac{\pi^2}{y^2} \right)^{-2} \quad \tilde{m} \equiv \frac{m}{m_{PQ}}, \quad y \equiv \frac{1}{m_{PQ} R}$$

CAST as a probe of LED

- a) $\delta=1$: $\sim 10^3$ KK states up to ~ 1 eV
- b) $\delta=2$: $\sim 10^6$ KK states up to ~ 1 eV

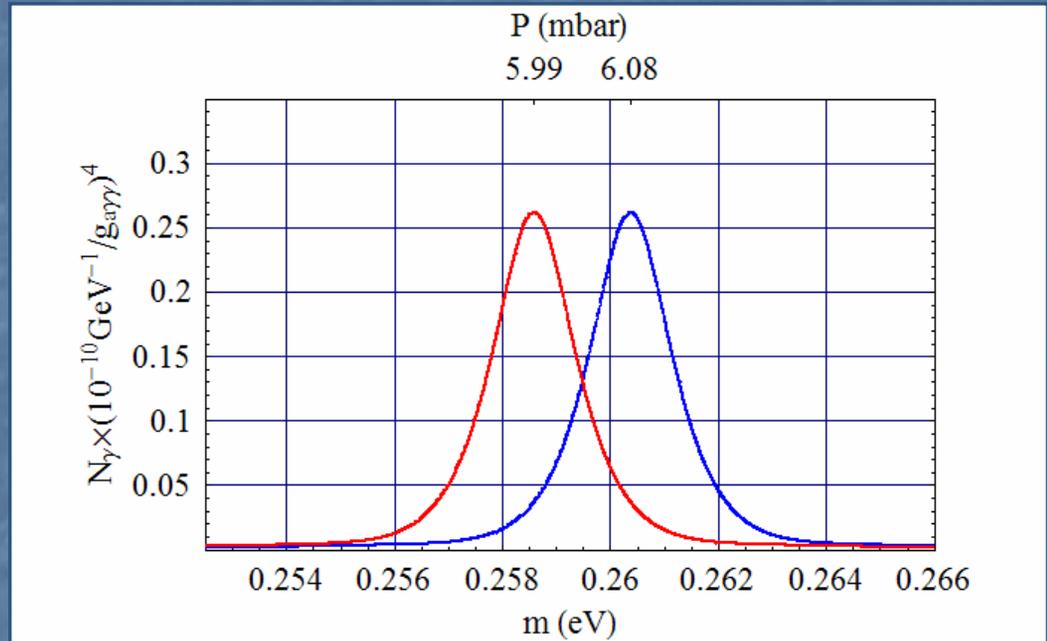
- at most an order of magnitude stringent limit
- the axion zero mode mass $m_a \approx 1/2R^{-1} = 6.6 \times 10^{-4}$ eV
- strong decrease in sensitivity on $g_{a\gamma\gamma}$ for $m_{PQ}R \gg 1$



CAST as a probe of LED

2) limits on the compactification radius R

- due to the coherence condition, CAST could be sensitive to particular KK states



- two signals while changing the pressure of the gas (in the regime $m_{\text{PQ}} < 1/(2R)$)

$$a) \quad m_a = m_{\text{PQ}} \quad \Rightarrow \quad m_1 = 1/R \approx 0.8 \text{ eV} \quad \Rightarrow \quad R \approx 250 \text{ nm}$$

$$b) \quad m_a = m_{\text{PQ}} \quad \Rightarrow \quad m_1 = 1/R \approx 1.15 \text{ eV} \quad \Rightarrow \quad R \approx 170 \text{ nm}$$

Conclusions

In addition to gravity, axions too could propagate in large extra space dimensions
⇒ Kaluza-Klein tower of axion states.

We have explored the potential of the CAST experiment for observing KK axions coming from the solar interior:

- In theories with two extra dimensions (with $R=0.15$ mm), **the axion mass is decoupled from f_{PQ}** and is set by the compactification radius R . In addition, there is a **strong decrease in sensitivity on $g_{a\gamma\gamma}$** for $m_{PQ}R \gg 1$ (due to mixing between the KK axion modes).
- CAST experiment may be sensitive to particular KK axions ⇒ probing of two large extra dimensions with a compactification radius R down to **170 nm** if $m_{PQ} < 1/(2R)$.



BACKUP SLIDES

Axions in LED

The mass matrix:

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$$M^2 = m_{\text{PQ}}^2 \begin{pmatrix} 1 & \sqrt{2} & \sqrt{2} & \sqrt{2} & \dots \\ \sqrt{2} & 2+y^2 & 2 & 2 & \dots \\ \sqrt{2} & 2 & 2+4y^2 & 2 & \dots \\ \sqrt{2} & 2 & 2 & 2+9y^2 & \dots \\ \vdots & \vdots & \vdots & \vdots & \ddots \end{pmatrix} \quad y = \frac{1}{m_{\text{PQ}} R}$$

The eigenvalues λ : the solutions to the transcendental equation

$$\pi R \lambda \cot(\pi R \lambda) = \frac{\lambda^2}{m_{\text{PQ}}^2}$$

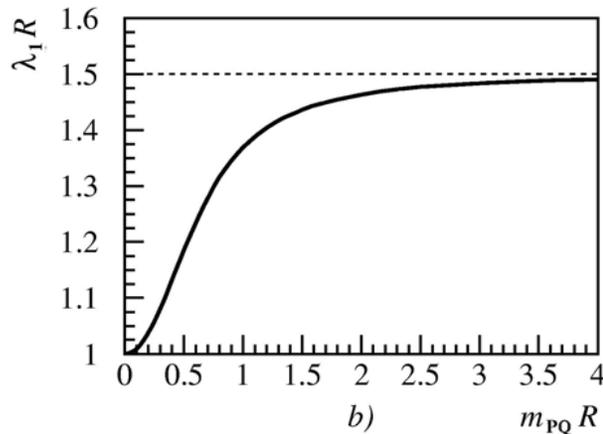
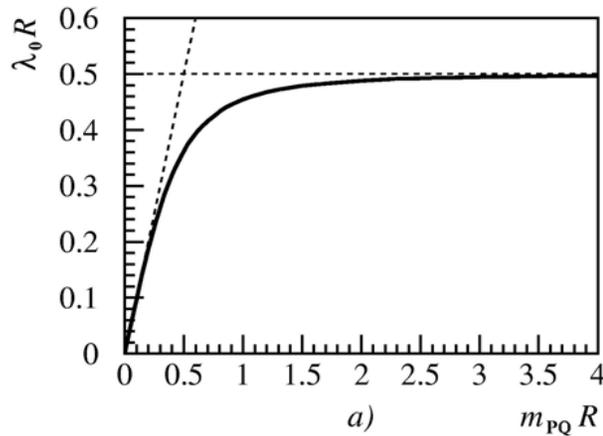
The axion linear superposition:

$$a' \equiv \frac{1}{\sqrt{N}} \sum_n r_n a_n = \frac{1}{\sqrt{N}} \sum_\lambda \tilde{\lambda}^2 A_\lambda \hat{a}_\lambda$$

$$A_\lambda \equiv \frac{\sqrt{2}}{\tilde{\lambda}} \left(\tilde{\lambda}^2 + 1 + \frac{\pi^2}{y^2} \right)^{-1/2} \quad \tilde{\lambda} \equiv \frac{\lambda}{m_{\text{PQ}}}$$

Axions in LED

- the solutions to the transcendental equation for a) the axion zero mode; b) the first KK excitation



- 1) if $m_{PQ} \ll \frac{1}{R}$ KK axion masses are $m_{PQ}, \frac{1}{R}, \frac{2}{R}, \dots$
- 2) if $m_{PQ} \gg \frac{1}{R}$ KK axion masses are $\frac{1}{2R}, \frac{3}{2R}, \frac{5}{2R}, \dots$

• the lightest axion mass eigenvalue

$$m_a \approx \min \left(m_{PQ}, \frac{1}{2R} \right)$$

• the masses of KK excitations are separated by $\approx 1/R$

